

054402 Design and Analysis**LECTURE 8: ADVANCED HEN SYNTHESIS**


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Schedule - Day Two

- **Unit 4. Loops and Splits**
 - Minimum Number of Units by Loop Breaking
 - Class Exercise 5 
 - Stream Split Designs
 - Class Exercise 6
- **Unit 5. Threshold Problems**
 - Class Exercise 7

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Part Two: Objectives

- This Unit on HEN synthesis serves to expand on what was covered last week to more advanced topics.
- Instructional Objectives - You should be able to:
 - Identify and eliminate "heat loops" in an MER design
 - Use stream splits to design for U_{min} and MER
 - Design a HEN for "Threshold Problems"

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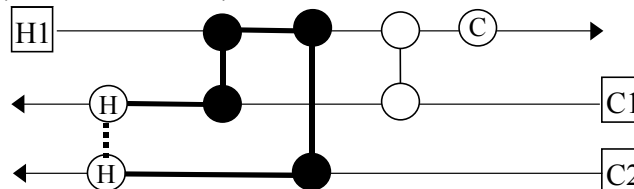
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UNIT 4: Loops and Splits

The minimum number of units (U_{min}) in a network:

$$U_{Min} = N_{Stream} + N_{Util} - 1 \quad (\text{Hohman, 1971})$$

A HEN containing U_{HEX} units ($U_{HEX} > U_{min}$) has $(U_{HEX} - U_{min})$ independent "heat loops".



The HEN above has 2 "heat loops"

Normally, when heat loops are "broken", heat flows across the pinch - the number of heat exchangers is reduced, but the utility loads are increased.

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Class Exercise 5 (Linnhoff and Flower, 1978)

Example:

Stream	T^S (°C)	T^T (°C)	ΔH (kW)	CP (kW/°C)
H1	180	40	280	2.0
H2	150	40	440	4.0
C1	60	180	360	3.0
C2	30	130	260	2.6

$$\Delta T_{\min} = 10 \text{ } ^\circ\text{C}.$$

Step 1: Temperature Intervals

(subtract ΔT_{\min} from hot temperatures)

Temperature intervals:

$$180^\circ\text{C} \Rightarrow 170^\circ\text{C} \Rightarrow 140^\circ\text{C} \Rightarrow 130^\circ\text{C} \Rightarrow 60^\circ\text{C} \Rightarrow 30^\circ\text{C}$$

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Class Exercise 5 (Cont'd)

Step 2: Interval heat balances

For each interval, compute:

$$\Delta H_i = (T_i - T_{i+1}) \times (\sum CP_{\text{Hot}} - \sum CP_{\text{Cold}})$$

Interval	H1	H2	C1	C2	T_i	$T_i - T_{i+1}$	$\sum CP_{\text{Hot}}$ $-\sum CP_{\text{Cold}}$	ΔH_i
1			█		180	10	-3.0	-30
2	█		█		170	30	-1.0	-30
3	█	█	█		140	10	3.0	30
4	█	█	█	█	130	70	0.4	28
5	█	█		█	60	30	3.4	102
6					30			

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Class Exercise 5 (Cont'd)

Step 3: Form enthalpy cascade.

This defines:
 Cold pinch temp. = 140 °C
 $Q_{rmin} = 60 \text{ kW}$
 $Q_{cmin} = 160 \text{ kW}$

	Assume $Q_H = 0$	Eliminate infeasible (negative) heat transfer $Q_H = 60$
$T_1 = 180^\circ\text{C}$		
$\Delta H = -30$		
$T_2 = 170^\circ\text{C}$	$Q_1 = -30$	30
$\Delta H = -30$		
$T_3 = 140^\circ\text{C}$	$Q_2 = -60$	0
$\Delta H = 30$		
$T_4 = 130^\circ\text{C}$	$Q_3 = -30$	30
$\Delta H = 28$		
$T_5 = 60^\circ\text{C}$	$Q_4 = -2$	58
$\Delta H = 102$		
$T_6 = 30^\circ\text{C}$	$Q_C = 100$	160

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Class Exercise 5 (Cont'd)

MER Design above the pinch: CP

$$U_{Min, MER} = N_{Stream} + N_{Util} - 1$$

$$= 2 + 1 - 1$$

$$= 2 \checkmark$$

MER Design below the pinch: CP

$$U_{Min, MER} = 4 + 1 - 1$$

$$= 4$$

MER design below pinch has 6 exchangers!
i.e. There are two loops below pinch.

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Class Exercise 5 (Cont'd)

Complete MER Design CP

However, $U_{\text{Min}} = N_{\text{Stream}} + N_{\text{Util}} - 1$
 $= 4 + 2 - 1$
 $= 5$

The MER network has 8 units. This implies 3 independent "heat load loops". We shall now identify and eliminate these loops in order to design for U_{Min}

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Class Exercise 5 (Cont'd)

Identification and elimination of 1st loop:

To reduce the number of units, the 80 kW exchanger is merged with the 60 kW exchanger. This breaks the heat loop, but also creates a ΔT_{min} violation in the network:

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Class Exercise 5 (Cont'd)

Identification and elimination of 1st loop (Cont'd):

To restore ΔT_{min} , the loads of the exchangers must be adjusted along a "heat path" by an unknown amount x . A "heat path" is a path through the network that connects heaters with coolers.

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Class Exercise 5 (Cont'd)

Identification and elimination of 1st loop (Cont'd):

Performing a heat balance on H1 in the exchanger which exhibits the ΔT_{min} violation:

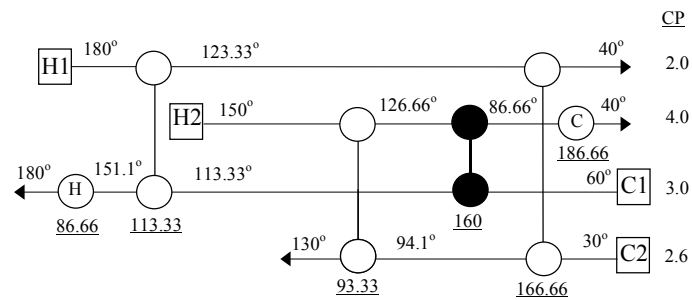
$$140 - x = 2(180 - 113.33 - \Delta T_{min}) \Rightarrow x = 26.66$$

This is called "energy relaxation"

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Class Exercise 5 (Cont'd)

Identification and elimination of 2nd loop:



Since there is no ΔT_{\min} violation, no adjustment of the loads of the exchangers is needed - we reduce the number of units by one with no energy penalty.

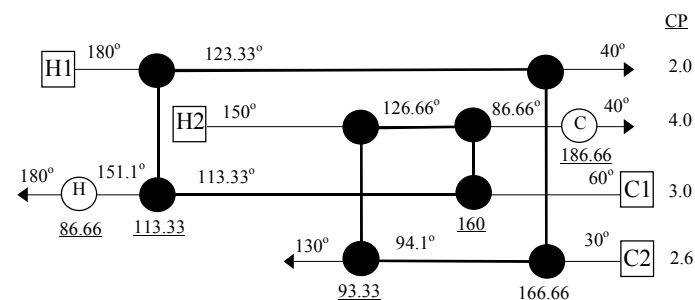
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Class Exercise 5 (Cont'd)

Identification and elimination of 3rd loop:

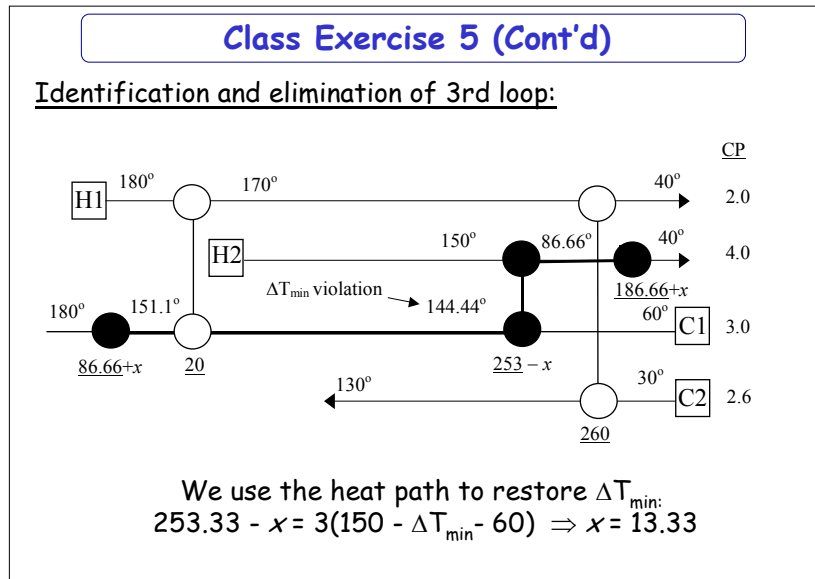


Shifting the load of the smallest exchanger (93.33 kW) around the loop, the network is reduced to...

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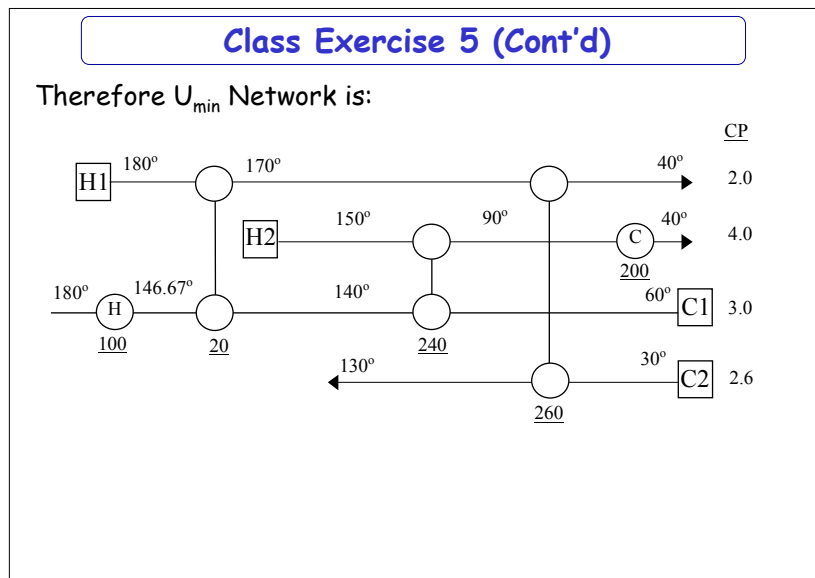
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Loop Breaking - Summary


Step 1:

Perform MER Design for U_{HEX} units. Try and ensure that design meets $U_{Min, MER}$ separately above and below the pinch.



Step 2:

Compute the minimum number of units:

$$U_{Min} = N_{Stream} + N_{Util} - 1$$

This identifies $U_{HEX} - U_{min}$ independent "heat loops", which can be eliminated to reduce U . 

Step 3:

For each loop, eliminate a unit.  If this causes a ΔT_{min} violation, identify the "heat path" and perform "energy relaxation" by increasing the duties of the cooler and heater on the heat path. 

Loops improve energy recovery and heat load flexibility at the cost of added units ($>U_{min}$)

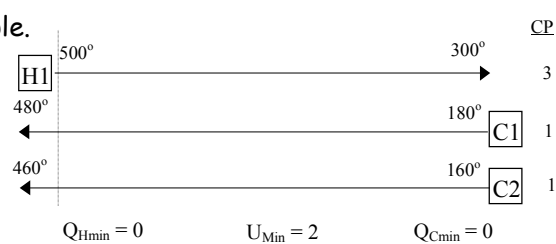
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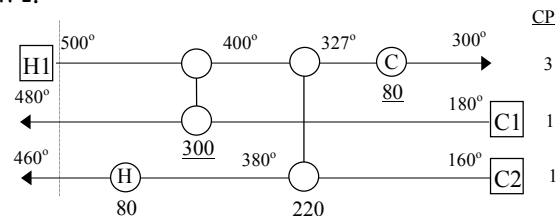
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Stream Split Designs

Example.



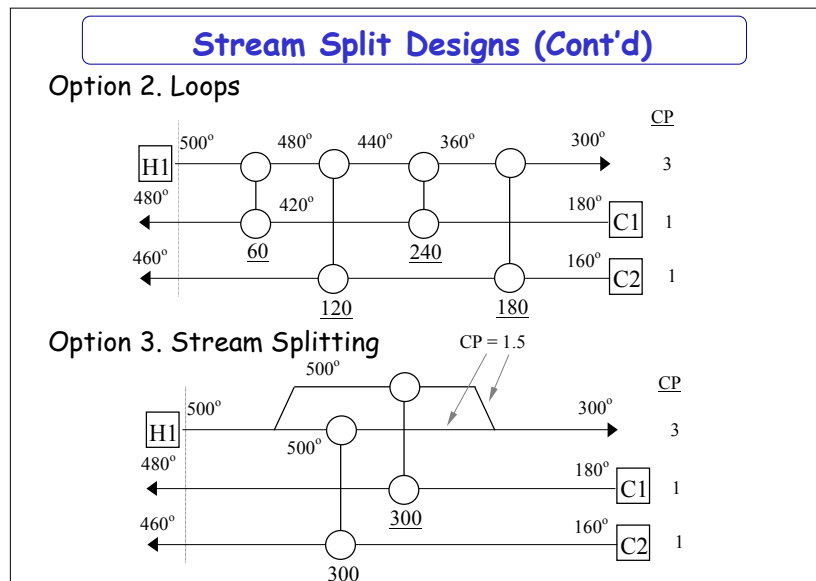
Option 1.



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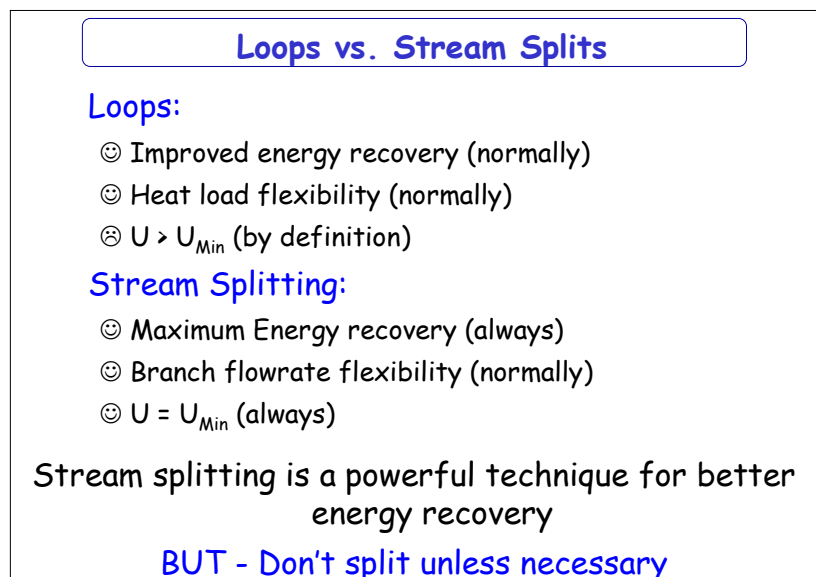
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Stream Splitting Rules

1. Above the pinch (at the pinch):

- ➔ ❶ Cold utilities cannot be used (for MER). So, if $N_H > N_C$, MUST split COLD streams, since for feasibility $N_H \leq N_C$
- ❷ Feasible matches must ensure $CP_H \leq CP_C$. If this is not possible for every match, split HOT streams as needed. If Hot streams are split, recheck ❶

2. Below the pinch (at the pinch):

- ➔ ❶ Hot utilities cannot be used (for MER). So, if $N_C > N_H$, MUST split HOT streams, since for feasibility $N_C \leq N_H$
- ❷ Feasible matches must ensure $CP_C \leq CP_H$. If this is not possible for every match, split COLD streams as needed. If Cold streams are split, recheck ❶

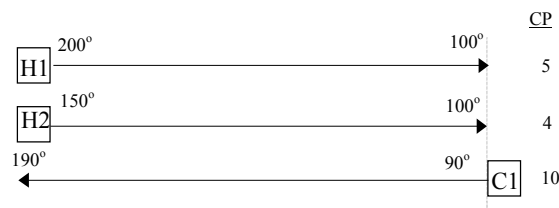
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Class Exercise 6

Design a hot-side HEN, given the stream data below:



Solution:

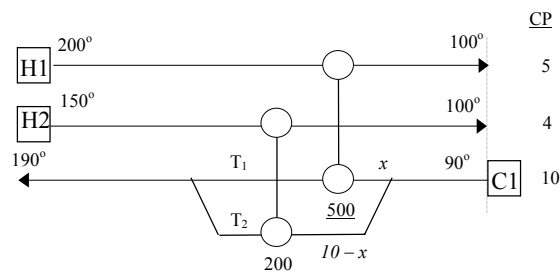
Since $N_H > N_C$, we must split C1. The split ratio is dictated by the rule: $CP_H \leq CP_C$ (necessary condition) and by a desire to minimize the number of units ("tick off" streams)

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Class Exercise 6 (Cont'd)



x is determined by the following energy balances:

$$x(T_1 - 90) = 500$$

$$(10 - x)(T_2 - 90) = 200$$

subject to: $200 - T_1 \geq \Delta T_{\min} = 10$

$150 - T_2 \geq \Delta T_{\min} = 10$

Best to make $T_1 = T_2$. Here, this is not possible. Why?

We shall make $T_2 = 140$ (why?)

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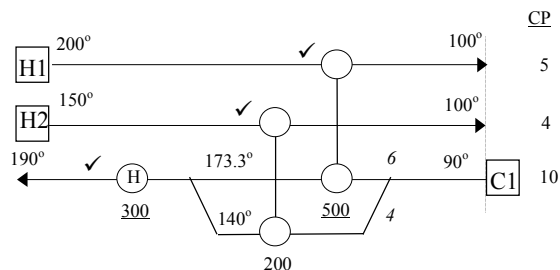
Class Exercise 6 (Cont'd)

A possible solution is therefore:

$$(10 - x)(140 - 90) = 200 \Rightarrow x = 6$$

$$T_1 = 90 + 500/x = 173.33 \text{ (satisfies constraint)}$$

Complete solution is:



This is an MER design which also satisfies U_{\min} ($U_{\min} = 3$).

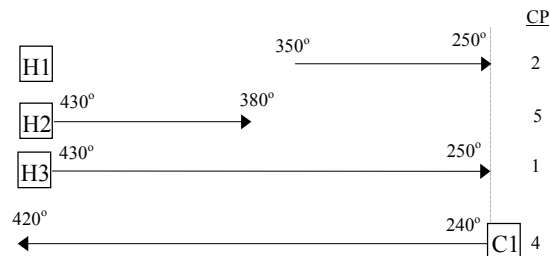
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Practice Exercise 1

Design a hot-side network for MER and U_{Min} given the stream data below.



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Practice Exercise 2

Data:

Stream	T^S (°F)	T^T (°F)	ΔH 10^4 kBtu/h	CP $(10^4 \text{ kBtu/h } ^\circ\text{F})$
H1	400	120	280	1.0
H2	340	120	440	2.0
C1	160	400	360	1.5
C2	100	300	260	1.3

$$\Delta T_{\text{min}} = 20 \text{ } ^\circ\text{F}$$

- ❶ Determine Q_{Hmin} , Q_{Cmin} and the pinch location.
- ❷ Design an MER network which satisfies energy targets
- ❸ Design a network for U_{Min} by eliminating the heat loops in the network and performing energy relaxation.

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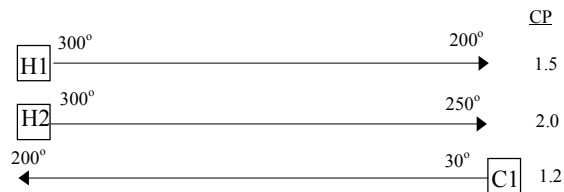
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UNIT 5: Threshold Problems

Networks with excess heat supply or heat demand may have MER targets with only one utility (i.e., either $Q_{Hmin} = 0$ or $Q_{Cmin} = 0$). Such designs are not separated at the pinch, and are called "Threshold Problems"

Example - Consider the problem



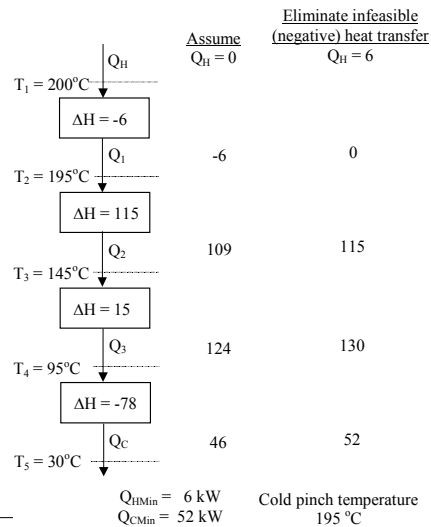
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Threshold Problems (Cont'd)

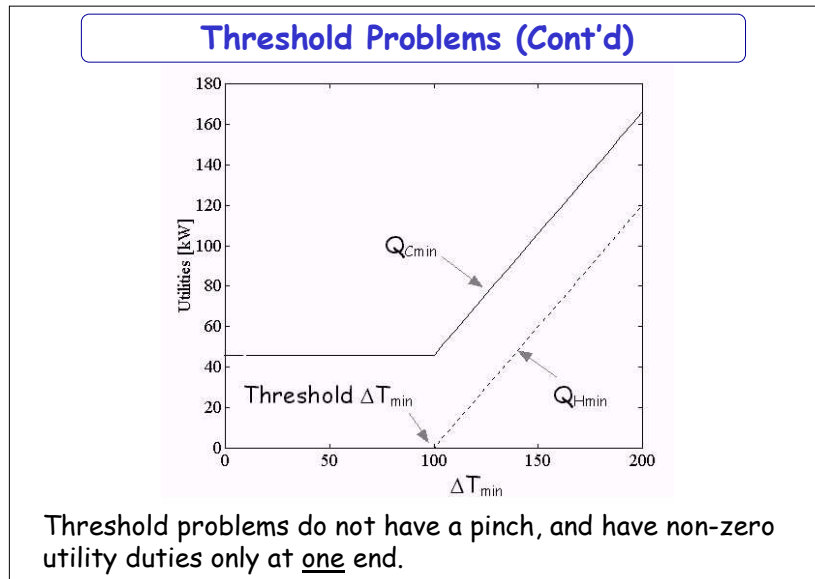
Assuming a value of $\Delta T_{min} = 105\text{ }^\circ\text{C}$:



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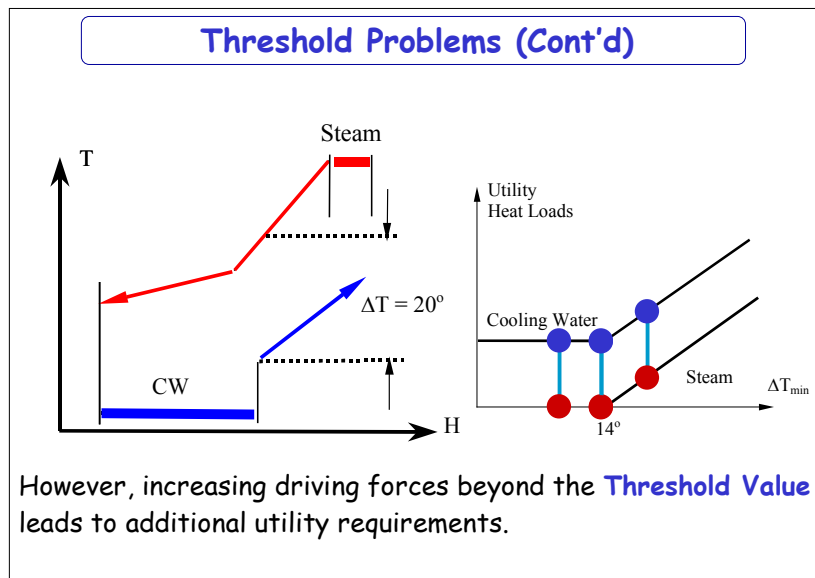
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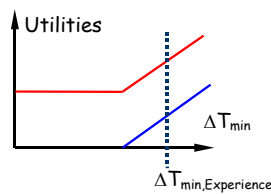
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Threshold Design Guidelines

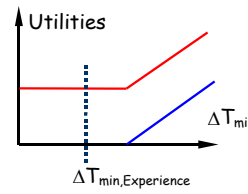
1. Establish the threshold ΔT_{\min}
2. Note the common practice values for ΔT_{\min} :

Application	Refrigeration	Process	Boiler
$\Delta T_{\min, \text{Experience}}$	1-2 °C	10 °C	20-30 °C

3. Compare the threshold ΔT_{\min} to $\Delta T_{\min, \text{Experience}}$
Classify as one of the following:



Pinched - treat as normal
pinched problem



Threshold - must satisfy target
temperatures at the "no utility end"

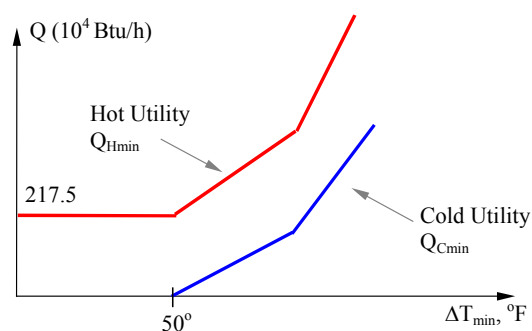
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Class Exercise 7

The graph shows the effect of ΔT_{\min} on the required levels of $Q_{H\min}$ and $Q_{C\min}$ for a process consisting of 3 hot and 4 cold streams.



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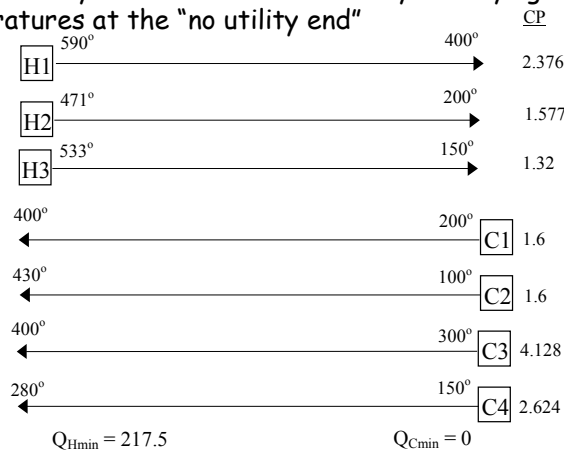
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Class Exercise 7 (Cont'd)

Design a network for U_{\min} and MER for the process.

Hint: Identify two essential matches by satisfying target temperatures at the "no utility end"



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Advanced HEN Synthesis - Summary

- **Unit 4. Loops and Splits**
 - Minimum Number of Units by Loop Breaking - U_{\min}
 - Stream Split Designs - U_{\min} and MER
- **Unit 5. Threshold Problems**
 - Problems with only hot or cold utilities (no pinch!)

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